Ray traced rendering using GPGPU devices

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ABSTRACT

Ray tracing is a very popular way to draw 3-D scenes onto a 2-D image. The technique produces a very high degree of visual realism with regard to shadows, reflection, and refraction. The drawback of this technique is the fact that it is extremely computationally expensive. This expense has been a barrier to using ray tracing to implement real-time rendering. Recent technological advances have fueled increased interest in the technique because the prospect of real-time ray tracing in commercial applications is now closer to becoming a reality. This thesis is an attempt to quantify the degree of speed-up, in terms of raw processing power, that this new class of GPU hardware makes possible.
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# Abstract

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1 INTRODUCTION

The first commercially available personal computer system to have a separate graphics processor apart from the CPU was the revolutionary Commodore Amiga. Since that time, the ever increasing popularity of video games, combined with market pressure for more realistic looking graphics, has driven the creation of very advanced graphics hardware that can perform faster than a CPU in many parallel computation tasks. The graphics card company NVidia was the first company to use the term Graphics Processing Unit, or GPU, as an acknowledgment that graphics cards had evolved into massively parallel computers that run alongside the main system CPU(s).

Traditionally, a GPU is a processor that is designed to perform the rapid execution of the traditional fixed graphics pipeline. The phrase “fixed graphics pipeline” refers to a graphics programming paradigm in which many operations that the graphics card executes are not alterable (programmable) by the programmer [16]. Rapid advances in GPUs have allowed more custom programmability of the GPU hardware as well as the addition of floating point capabilities in 2003 [12]. As a consequence, the fixed graphics pipeline has been superseded by user-programmable pipelines in which the API allows users to write code for parts of the pipeline known as shaders [30]. These APIs do a better job of utilizing the full computing power of this programmable graphics hardware. This has allowed for the computational power of the graphics card to be used in new ways. For instance, it is now possible to leverage the GPU to perform general-purpose parallel computation tasks that do not necessarily have anything to do with any graphics pipeline [14], [8].

Additionally, parallel computation has received increased attention due to the current limitations that have been encountered with attempts to increase the speed of single-core CPUs, namely the ability to dissipate heat quickly enough [15], [5]. Newer CPUs have achieved greater processing power while avoiding heat problems by increasing the number of processor cores instead of increasing the processor’s frequency.

OpenCL is an API that has been written to utilize multicore processors of all types, including GPUs, to facilitate parallel processing in a heterogeneous processor environment. It allows a programmer to develop code in an ANSI C99-based language which can be compiled for multiple different processor architectures [17], [22], [23]. This is another way of saying that OpenCL code that is written against one type of GPU should run against another with little or no modification of code. By comparison, earlier GPU programming languages suffer from portability issues and require extensive practice to master [10], [14], [6], [25]. This thesis describes the process of implementing a ray tracing [1] algorithm in OpenCL, utilizing a Radeon Mobility 5870 GPU as the computation device.
2 RELATED WORK

There is a large amount of research directed toward the problem of increasing the speed of ray tracing through various parallelization attempts in GPU hardware [19], [9] as well as in other types of hardware [20]. These research activities have helped to motivate the current interest level in GPGPU technology.

Some papers have alluded to the fact that OpenCL’s cross-platform capabilities come at the cost of some performance [12], [15]. In other words, multiple research projects have reaffirmed what the Computer Science community has learned from experience – these early attempts at cross-platform technology often result in a performance loss when compared to custom low-level implementations [7]. However, this should not detract from the importance of the exercise of developing and using cross-platform technology that works seamlessly across different hardware platforms. The benefits have been shown to outweigh the cost in most development scenarios.

3 RAY TRACING FUNDAMENTALS

The sections that follow provide the necessary background on ray tracing so that one can better understand the results of this project.

3.1 RENDERING

In computer graphics, the process of drawing 3-D geometry to a 2-D screen image in such a way that it appears 3-D with appropriate colors is called rendering. There is more than one way to achieve this effect. One very popular technique is called ray tracing, which is the technique used in this project. The reason for ray tracing’s popularity stems from the fact that the algorithm’s recursive nature makes it simple to implement. The technique also provides very accurate reflections, shadows, and refraction to a degree that is above and beyond what other rendering methods provide. Before a more in-depth discussion of ray tracing, it is necessary to define a few terms:

**Image plane** – The mathematical plane on which the ray-traced image will be drawn.

**View frustrum** – The 3-D volume in space that includes all visible objects which will be projected onto the image plane during rendering.

**Pixel** – Abbreviated term for picture element. It is the smallest addressable region of 2-D space on a computer monitor. Each pixel is represented in the frame buffer by a 32-bit integer (in most present-day scenarios).

**Frame buffer** – A memory location, usually on the graphics card, where color data used to set pixel colors is stored, usually in the form of a large array of 32-bit integers. For each 32-bit integer in the frame
buffer, the first 8 bits represent the red component of a color, the second 8 bits represent the green component of the color, and the third 8 bits represent the blue component of the color. The final 8 bits are used for purposes that are outside the scope of this project.

It may be worthwhile to note that, conceptually, ray tracing is very similar to the behavior of light in a pinhole camera [26]. In the case of a pinhole camera, light enters a hole in an otherwise light-proof box and strikes film on the back of the box. This process of photons hitting this film creates an image of what is in front of the pinhole. The image plane is comparable to the pinhole camera film. The camera is comparable to the pinhole. A key difference between the image plane and the pinhole camera film is that the image plane is in front of the camera instead of behind it, resulting in an image that is not inverted [26]. In contrast, the camera film is behind the pinhole, which inverts the image on the film. Figure 1 shows the comparison of a pinhole camera to ray tracing concepts.

FIGURE 1 - FOUNDATIONAL RAY TRACING CONCEPTS

3.2 Ray Tracing

Imagine a room with a single source of light and multiple objects in it. The light source will emit photons, and each photon will travel on a path known as a light ray. These photons will strike objects and re-emit from the surface of those struck objects. Each such interaction is essentially a “reflection”. In this way, photons will bounce around the entire scene until they run out of energy. Objects can be directly lit by a light source or indirectly lit from a reflection off of another object. Let’s say that there is a camera in the scene oriented in space. Some photons will enter the camera lens, and some photons will not. The
photons that enter the camera lens contribute to the image seen by the camera. Determining the path that a photon takes as it travels around a scene is what is known as ray tracing [26].

### 3.3 Forward Ray Tracing

Forward ray tracing is a particular kind of ray tracing that follows the path that photons take from their light source. The “forward” aspect of this naming refers to the fact that we are keeping track of the path photons take on their journey from their light source as they enter the room. This is an accurate but wasteful approach because photons that do not enter the camera lens do not contribute to the constructed image. The sheer number of photons that do not reach the camera lens but need to be traced results in an extremely time-consuming algorithm [26].

### 3.4 Backward Ray Tracing

The solution to this wastefulness is to only consider the photons that contribute to the image (i.e., enter the camera lens). We do this by reversing the ray tracing problem and trace photon paths starting from the camera, moving backward into the scene. The process of backward ray tracing begins with the assumption that all photons that strike the image plane will be photons that contribute to the image. A convenient way to model this reverse light ray is with the mathematical concept of a ray, which has both a starting point and a direction. To calculate the color of every pixel on the screen, we extend a ray through every pixel-sized portion of the image plane and use the ray tracing algorithm to retrieve the color for that pixel [26]. The ray is mathematically defined below.

**Ray** – A ray is mathematical line used to model the path of light rays in a 3-D volume. It is expressed parametrically as \( R(t) = O + tD \) where:

\[ R(t) \] represents the ray.

\[ O \] represents the ray origin point.

\[ D \] represents the normalized ray direction vector.

\( t \) represents a scalar multiplier (parameter) that determines a particular location on the ray. It has a valid range of \([0, \infty)\).

### 3.5 Ray Generation

The process of determining the x-y coordinates through which to extend a ray is a matter of finding the pixel center for each considered pixel on the image plane. This process is a substantial part of ray generation. In order to best explain how to generate rays, it is useful to consider a simplified scenario that
uses a fictitious monitor resolution of 6 pixels. We will map the image plane onto these 6 pixels to show how it is done; a real screen resolution has many more pixels, of course.

A fast way of determining the center of a pixel is to calculate the pixel’s width and height on the image plane.

In order to calculate these two values, we need the image plane dimensions and the monitor resolution dimensions. Let’s say that the image plane X dimension (width) is [-15, 15] in world coordinates and the image plane Y dimension (height) is [-10, 10] in world coordinates. The screen resolution dimensions are 3 pixels by 2 pixels, comprising our 6-pixel monitor resolution.

\[
\text{pixel width} = \frac{15 - (-15)}{3 \text{ pixels}} = \frac{30}{3 \text{ pixels}} = 10 \text{ units in world coordinates}
\]

\[
\text{pixel height} = \frac{10 - (-10)}{2 \text{ pixels}} = \frac{20}{2 \text{ pixels}} = 10 \text{ units in world coordinates}
\]

Now that these values are calculated, it is clear that a pixel is 10x10 units on our image plane. With this information and the lower-left coordinates of the image plane, we can calculate the x-y location of the first pixel on the image plane. Since it is most accurate to have the ray pierce the center of each 10x10 square on the image plane that represents a pixel, we add 5 to each dimension (x and y) of the lower-left coordinate of the image plane. In doing so, the ray pierces the center of the first pixel instead of the lower-left corner of the first pixel.

The step-by-step process for determining the x-y coordinates for each pixel will now be explained in detail. We start with:

Left-most X = -15
Bottom-most Y = Image plane bottom = -10

Adjust left-most X and bottom-most Y so that they are centered in the image plane area corresponding to the first pixel.

Current pixel X = Left-most X + 5
Current pixel Y = Bottom-most Y + 5

Now we are in the center of the first pixel.
Pixel 1 = (Current pixel X, Current pixel Y) = (-10, -5)

Add **pixel width** to get to the next pixel.

    Current pixel X = Current pixel X + **pixel width**

Pixel 2 = (Current pixel X, Current pixel Y) = (0, -5)

Add **pixel width** to get to the next pixel.

    Current pixel X = Current pixel X + **pixel width**

Pixel 3 = (Current pixel X, Current pixel Y) = (10, -5)

Now we move up a row to map the upper portion of image plane to the next row of pixels starting at pixel 4. To complete the calculations, apply the same process in the y-dimension, then move across the new row in the same way.

As can be seen, the constants **pixel width** and **pixel height** facilitate efficient calculation of the next pixel location, which amounts to one addition operation in all cases except a pixel row change. Now that we have our x-y coordinates for the ray piercings, we need to choose a position down the z-axis for the image plane to reside. Since we are using the right-handed coordinate system, the negative direction on the z-axis can be thought of as the forward direction from the camera origin that is perpendicular to the image plane. As a consequence, our image plane will exist at a negative coordinate on the z-axis. The closer the image plane is to the origin, the more the camera will exhibit a wide-angle lens effect. The farther the image plane is from the origin, the more the camera will have the effect of a narrow lens. In this project, we use an image plane location of -9 on the z-axis.

Now the \((x, y, z)\) locations of the ray piercings for each pixel are:

- Ray 1 pierce location = \((-10, -5, -9)\)
- Ray 2 pierce location = \((0, -5, -9)\)
- Ray 3 pierce location = \((10, -5, -9)\)
- Ray 4 pierce location = \((-10, 5, -9)\)
- Ray 5 pierce location = \((0, 5, -9)\)
- Ray 6 pierce location = \((10, 5, -9)\)
Next, we need to calculate the rays. For each ray, we start with the origin at \((0, 0, 0)\) and use its ray pierce location and the origin to calculate its \(D\) vector, which is then normalized. Once we have the parametric ray equation for all six rays, we can use these rays to ray trace. The image plane of Figure 2 shows the \(X\) and \(Y\) locations on the plane where each of the 6 rays will pierce the plane, represented as dots. The left portion of the figure shows the corresponding pixels and the order in which they are mapped to the image plane. While a 6-pixel resolution is highly unlikely in real-world instances, this algorithm is applicable to a screen resolution of any number of pixels and to any image plane(window) size.

**FIGURE 2 - MAPPING A HYPOTHETICAL 6 PIXEL MONITOR TO 30X20 IMAGE PLANE**

### 3.6 Ray Tracing Algorithm

Before discussing the ray tracing algorithm, it is necessary to define some terms:

**Polygonal mesh** - A polygonal mesh is a collection of vertices, edges, and faces that defines the shape of a 3-D object in 3-D computer graphics.

**Bounding sphere** - A bounding sphere is the smallest enclosing sphere that surrounds each polygonal mesh in the scene. It is used to accelerate intersection testing with the bounded polygonal object.

The ray tracing algorithm is as follows:

For each pixel on the screen:

1. Calculate a primary ray that originates at the virtual camera lens and goes through the location on the image plane associated with the center of the current pixel. This is the process that was covered in the previous section.
1) For each bounding sphere, determine whether a ray intersects with the sphere.
   a. If the ray intersects the current sphere, intersection tests need to be performed against all triangles inside the bounding sphere.
      i. If an intersection with a triangle has occurred and it is the closest found so far, record it as the closest.
   b. If the ray does not intersect the current sphere, go to the next sphere in the list and proceed to step 1a.

2) If the ray did not intersect any triangles, set the current pixel to the background color, go to the next pixel and return to step 0, otherwise continue to step 3.

3) Determine the shade (color) at the intersection point of the ray with the triangle.
   This process is known as shading. The steps for shading are as follows:
   a. Obtain a color value using the Phong Illumination Model of Section 4.3.
   b. When calculating a shade value at an intersection point, do not include lighting contributions from any light which is obstructed by another object. In order to determine whether an intersection point is shadowed, we need to determine whether any light sources contributing to the shade value of that location are obstructed by another object. To accomplish this, we cast a shadow ray from the intersection point to each light source. We then apply our sphere and triangle intersection routine to each ray in order to determine whether the ray intersects with another object on its way to the light source. If any ray intersects with an object, we know that the particular light source we are testing is obstructed by the intersected object. Each obstructed light source does not contribute to the shade value at the intersection point. Figure 3 shows an example of an obstructed light source and an unobstructed light source.
c. Obtain color contributions from reflections. Once a ray actually hits a surface, there will be a reflected ray. This ray may or may not strike another object. If the reflected ray does strike another object, the color of the struck object at the point it is intersected by the ray will be added to the color of the original intersection point as a percentage contribution to that intersection point’s color. In the unmodified ray trace algorithm, this reflection process is recursive. In this project, however, the reflection is limited to one reflected ray per primary ray because OpenCL kernels do not allow recursion and the iterative version of this algorithm is very complex.
4) If the current pixel is the last pixel, terminate the algorithm, otherwise go to the next pixel and return to step 0.

4 ALGORITHM MATHEMATICS

The mathematical operations for the ray tracing algorithm are visited in the sections that follow.

4.1 INTERSECTION CALCULATIONS

The following sections detail the first major step of the ray tracing algorithm – finding the closest point at which the ray intersects with an object.

4.1.1 SPHERE INTERSECTION

In terms of computational time, trying to intersect a ray with a list of triangles that comprise an object takes much longer than intersecting with a single bounding sphere. For example, if an object is constructed using 40,000 triangles, we would need to attempt to intersect with all of the triangles to determine which triangles, if any, have been intersected. For this reason, an optimization step that involves first intersecting with a bounding sphere is desirable. Intersecting with a bounding sphere is much less costly than intersecting with a triangle and is only a single intersection calculation. In contrast, in the absence of bounding spheres, we would need to perform intersection calculations with all triangles in the scene. Unless the number of triangles comprising our scene’s objects is very small, this will result in many expensive triangle intersection calculations for triangles that are nowhere near the ray we are testing. If the ray does not intersect with any of the triangles, all the computation that has been attempted is wasteful.

Below are the calculations for performing ray intersection with a sphere:

The ray \( R(t) \) with origin point \( O \) and direction vector \( D \) can be written parametrically as:

\[
R(t) = O + t D \quad t > 0 \tag{1}
\]

The function \( R(t) \) represents a point on the ray for any specific value of \( t \).

\[
D = (X_{\text{dir}}, Y_{\text{dir}}, Z_{\text{dir}}) \tag{2}
\]

\[
X_{\text{dir}}^2 + Y_{\text{dir}}^2 + Z_{\text{dir}}^2 = 1 \tag{3}
\]

This is true because the direction vector is a normalized vector.

The equation for the sphere is:
Sphere radius: \( S_r \) \hspace{1cm} (4)

Sphere Center: \( S_{\text{center}} = (X_c, Y_c, Z_c) \) \hspace{1cm} (5)

A point on the surface of the sphere \((X_s, Y_s, Z_s)\) is given by:

\[
(X_s - X_c)^2 + (Y_s - Y_c)^2 + (Z_s - Z_c)^2 = S_r^2
\] \hspace{1cm} (6)

Since the intersection point on the sphere is also a point on the ray we can rewrite the ray equation to express a candidate sphere surface point in terms of the ray:

\[
X = X_o + X_{\text{dir}} \cdot t
\]

\[
Y = Y_o + Y_{\text{dir}} \cdot t
\]

\[
Z = Z_o + Z_{\text{dir}} \cdot t
\]

We now substitute these equations for \((X_s, Y_s, Z_s)\) in equation (6). We solve for \( t \) to test whether the point is on the sphere.

\[
(X_o + X_{\text{dir}} \cdot t - X_c)^2 + (Y_o + Y_{\text{dir}} \cdot t - Y_c)^2 + (Z_o + Z_{\text{dir}} \cdot t - Z_c)^2 = S_r^2
\]

Equation (8) can be written as a quadratic equation in \( t \) as:

\[
A \cdot t^2 + B \cdot t + C = 0
\] \hspace{1cm} (9)

The coefficients \( A, B, \) and \( C \) are in terms of the sphere and the ray and can be computed:

\[
A = X_{\text{dir}}^2 + Y_{\text{dir}}^2 + Z_{\text{dir}}^2 = 1
\] \hspace{1cm} (10)

\[
B = 2 \cdot (X_{\text{dir}} \cdot (X_o - X_c) + Y_{\text{dir}} \cdot (Y_o - Y_c) + Z_{\text{dir}} \cdot (Z_o - Z_c))
\]

\[
C = (X_o - X_c)^2 + (Y_o - Y_c)^2 + (Z_o - Z_c)^2
\]

Solving (9) using the quadratic formula, with \( A = 1 \):

\[
t_0 = \frac{-B - \sqrt{B^2 - 4AC}}{2}
\] \hspace{1cm} (11)

\[
t_1 = \frac{-B + \sqrt{B^2 - 4AC}}{2}
\]

If \( B^2 - 4 \cdot C < 0 \), the ray does not intersect the sphere because there are no real roots and hence no solution that can be used in the ray equation. This essentially means that the ray does not intersect the sphere.
If $B^2 - 4 \cdot C \geq 0$, we take the following steps:

1) Make sure either or both of $t_0$ and $t_1$ are positive to ensure that at least one surface of the sphere is intersected. Negative $t$ values indicate sphere intersections that occur behind the ray origin and are not valid intersections as a consequence.

2) The smallest positive $t$ value of $t_0$ and $t_1$ represents the closest intersection point with the sphere along the ray. Take this smallest positive value and use it to calculate the intersection point by substituting the value into the ray equation.

$$X_{\text{intersection}} = X_o + X_d \cdot t$$

$$Y_{\text{intersection}} = Y_o + Y_d \cdot t$$

$$Z_{\text{intersection}} = Z_o + Z_d \cdot t$$

### 4.1.2 Sphere Surface Normal Vector

The sphere surface normal vector is required when rendering the bounding spheres of the scene rather than the objects inside the spheres. Rendering the bounding spheres is often helpful in testing a ray tracer to make sure that the spheres and their enclosed objects are located where they are believed to be in three-dimensional space. We need to define one new term, $S_n$:

$S_n$ stands for a normalized sphere surface normal vector at the specified intersection point.

$$S_n = \left( \frac{X_{\text{intersection}} - X_c}{S_r}, \frac{Y_{\text{intersection}} - Y_c}{S_r}, \frac{Z_{\text{intersection}} - Z_c}{S_r} \right)$$

### 4.1.3 Triangle Intersection

Upon successful determination that a ray has entered a polygonal mesh’s bounding sphere, triangle intersection tests are performed against all the triangles in the object’s polygonal mesh. The triangle intersection algorithm used in this project is the Moller-Trumbore triangle intersection algorithm [28]. An excerpt of the derivation that calculates the triangle intersection point is listed below.

Recall that ray $R(t)$ with origin $O$ and direction $D$ can be written parametrically as:

$$R(t) = O + tD \quad \text{(1)}$$

The function $R(t)$ represents a point on the ray for any specific value of $t$.

A point on the triangle in terms of barycentric coordinates $u$ and $v$ is given by:
\[ T(u, v) = (1 - u - v)V_0 + uV_1 + vV_2 \]  \hspace{1cm} (2)

Given the above, the ray will intersect with the triangle when \( R(t) = T(u, v) \). So we would like to find out what values of \( t, u, \) and \( v \), if any, make that equality true.

Substituting:

\[ 0 + t\mathbf{D} = (1 - u - v)V_0 + uV_1 + vV_2 \]  \hspace{1cm} (3)

Rearranging terms and expressing the left side in matrix form yields:

\[
\begin{bmatrix}
-D & V_1 - V_0 & V_2 - V_0
\end{bmatrix}
\begin{bmatrix}
t \\
u \\
v
\end{bmatrix}
= O - V_0
\]  \hspace{1cm} (4)

If we let \( M = \begin{bmatrix}
-D & V_1 - V_0 & V_2 - V_0
\end{bmatrix} \) then the algebraic solution to (4) can be written as:

\[
M^{-1} \begin{bmatrix}
t \\
u \\
v
\end{bmatrix} = M^{-1} (O - V_0)
\]  \hspace{1cm} (5)

Since \( M^{-1} \) is just the identity matrix, we are left with:

\[
\begin{bmatrix}
t \\
u \\
v
\end{bmatrix} = M^{-1} (O - V_0)
\]  \hspace{1cm} (6)

Using Cramer’s rule and some linear algebra rules, it can be shown that the solution in terms of triangle vertices and the ray components is:

\[
\begin{bmatrix}
t \\
u \\
v
\end{bmatrix} = M^{-1} (O - V_0) = \frac{1}{(\mathbf{D} \times (V_2 - V_0)).(V_1 - V_0)} \begin{bmatrix}
((O - V_0) \times (V_1 - V_0)) \times (V_2 - V_0) \\
((O - V_0) \times (V_1 - V_0)) \times (V_2 - V_0)
\end{bmatrix}
\]  \hspace{1cm} (7)

The triangle is intersected by the ray if \( 0 \leq u \leq 1, 0 \leq v \leq 1, u + v \leq 1 \). Otherwise, the ray missed the triangle. If the ray does hit the triangle, \( t \) is used in the ray equation to calculate the intersection point. The \( u \) and \( v \) parameters are used to interpolate the normal that will be used when we discuss the Phong Shading Model.

### 4.1.4 Triangle Surface Normal Vector

Calculating the triangle surface normal vector at a particular intersection point is more involved than calculating the surface normal vector of the sphere. There is one normal vector associated with each triangle vertex. We must interpolate the intersection point’s normal vector from all three of these vertex normal vectors. The interpolation is performed using the \( u \) and \( v \) values obtained from the triangle intersection step of the previous section. As Figure 5 shows, \( u, v \) and \( 1 - u - v \) represent the distances of
any point on the triangle from its vertices. Since they can be viewed as weighting values, they are also used to interpolate vertex normal vectors, vertex color, and vertex texture coordinates. The interpolation of the surface normal vector at the intersection point is as follows:

Let us call the three normal vectors associated with the triangle vertices $N_1, N_2, N_3$.

Then the triangle normal vector at the intersection point is:

$$
T_{nx} = (1 - u - v)N_{2x} + (uN_{1x}) + (vN_{3x})
$$

$$
T_{ny} = (1 - u - v)N_{2y} + (uN_{1y}) + (vN_{3y})
$$

$$
T_{nz} = (1 - u - v)N_{2z} + (uN_{1z}) + (vN_{3z})
$$

The surface normal vector at the intersection point is interpolated using $u$, $v$, and the 3 vertex normal vectors.

**FIGURE 5 - RELATIONSHIP BETWEEN VERTEX NORMALS AND BARYCENTRIC COORDINATES U AND V**

Normalize:

$$
T_{\text{length}} = \sqrt{T_{nx}^2 + T_{ny}^2 + T_{nz}^2}
$$

$$
T_{nx} = \frac{T_{nx}}{T_{\text{length}}}
$$

$$
T_{ny} = \frac{T_{ny}}{T_{\text{length}}}
$$

$$
T_{nz} = \frac{T_{nz}}{T_{\text{length}}}
$$
4.2 Phong Shading Model

There are multiple approaches to shading. One of the earlier approaches is known as Gouraud shading. It is calculated by interpolating vertex color across a polygon. The left-most monkey head in Figure 6 shows the gradual brightness gradient produced by Gouraud shading, particularly with respect to the monkey’s nose area.

In contrast, the Phong shading model requires that a separate shade value be calculated at each point on a triangle’s surface. Thus, the normal vector at each point in a triangle is a weighted sum of the normal vectors at the triangle’s vertices. Each of these calculated normal vectors are then used to calculate a separate shade. The middle monkey head of Figure 6 shows an example of Phong shading. The net effect of recalculating a shade value at each intersection point is that the drop-off in brightness starting from the center of the monkey’s nose is much more pronounced in Phong shading than it is for the vertex color interpolation of Gouraud shading – meaning shininess is more obvious.

FIGURE 6 - GOURAUD SHADING (LEFT) VS RAY TRACED PHONG SHADING (MIDDLE) ALONG WITH UNDERLYING GEOMETRY (RIGHT)

4.3 Phong Illumination

Phong Illumination attempts to model the way light interacts with a surface. Its calculations are performed using the normal vector obtained from the calculations of the Phong shading model. Within the Phong illumination model, there are two categories of properties that generate the color at an intersection point: light properties and material properties. Light reflected from a surface is arbitrarily broken down into three components: diffuse, specular, and ambient. These reflections will be discussed in the following sections but some definitions are first necessary.

Reflection coefficient – A reflection coefficient is a way to model the degree to which a particular material reflects or absorbs light of different wavelengths. Thus, reflection coefficients determine the color of the reflection. The range of this value is [0,1] and is multiplied by the corresponding light property’s value. These coefficients effectively act as scaling values for light intensities.
**Light Intensity** – A light intensity in the Phong Illumination Model captures the color and brightness of the specular, diffuse, or ambient component of a light source. The model allows for the color of each of these components to be different but in physical reality the colors of each of these components are the same.

It is worthwhile to note that although these categorizations of light produce realistic looking results in the Phong illumination model, they are not an accurate portrayal of the way light behaves in nature. In reality, light has a color determined by an energy level. Certain materials reflect some colors better than others and the effects of this will be seen in the reflected color. This physical behavior is what the “material color”, expressed using $K_d$, $K_a$, and $K_s$, is modeling [26].

4.3.1 **Diffuse Reflection**

Diffuse light is reflected in all directions and originates from active light sources. The theoretical foundation for the diffuse reflection calculation is Lambert’s Law. This law states that the cosine of the angle between the normal vector $\mathbf{N}$ of the surface intersection point on the polygon and the normalized light vector $\mathbf{L_s}$ extending from the intersection point to the light source $\mathbf{L_s}$ is directly proportional to the brightness of the diffuse reflection. Therefore, the total diffuse contribution of the shade value at a given intersection point is determined by adding up the diffuse reflections from all light sources using Lambert’s Law. The cosine of the angle between any two normalized vectors is the dot product of those vectors. For any given light source, we take the dot product of the normalized light vector and the intersection point’s surface normal vector to calculate the cosine of the angle between them. We then take the resultant value and multiply it by the material’s diffuse reflection coefficient $K_d$ and the light’s diffuse intensity $I_{L_s,d}$. Remember that the dot product, or cosine, between two normalized vectors is closer to 0 if the angle between the vectors is near 90 degrees. The dot product is closer to 1 if the angle between the normalized vectors is small. In other words, when the normalized light vector and the normal vector are closer, the diffuse reflection will be more intense. It is important to note that the diffuse reflection does not depend on the view direction, and the reflection is most intense along the normal vector. The view direction is not included in the calculation because the diffuse reflection scatters in all directions. The diffuse term is defined below.

$$K_d (\mathbf{L_s} \cdot \mathbf{N}) I_{L_s,d}$$

4.3.2 **Specular Reflection**

Specular light is caused by mirror-like reflections off a smooth surface. This type of light results in shiny spots on objects. The specular reflection was developed by Bui Tuong Phong [32]. Like the diffuse contribution, the total specular reflection of the shade value is determined by adding up the specular contributions from all light sources. The normalized reflection vector $\mathbf{R}_{L_s}$ results from the light source $\mathbf{L_s}$ reflecting off the intersection point about the normal vector $\mathbf{N}$. The specular reflection is
maximized when the normalized view vector $\mathbf{V}$ which points from the intersection point toward the viewpoint and the normalized reflection vector $\mathbf{R}_{ls}$ are aligned, and it drops off when $\mathbf{V}$ is not near $\mathbf{R}_{ls}$. That is, it is another calculation that involves determining the cosine of the angle between two vectors in order to derive light intensity. As a consequence, we take the dot product of the intersection point’s reflection vector and the view vector.

$\alpha$ is a shininess constant for the material. Material shininess captures where on the spectrum of shininess the material falls. Its value models the smoothness of a surface ranging from very coarse to very smooth. A smoother surface corresponds to a more perfectly reflective surface and a smaller specular highlight (shiny spot). A coarser surface corresponds to a less perfectly reflective surface and has larger specular highlights as a result, since light scatters in many directions. The dot product calculation is raised to this shininess constant. Next, the specular reflection coefficient $K_s$ and specular light intensity $I_{ls,s}$ are both multiplied into the current equation as shown below.

$$K_s (\mathbf{R}_{ls} \cdot \mathbf{V})^\alpha I_{ls,s}$$

### 4.3.3 Ambient Reflection

Ambient light is light whose source cannot be determined easily. It is intended to model scattered environmental light and can thought of as a sort of “brightness adjustment”. Ambient reflection is calculated by multiplying the ambient light intensity $I_a$ by the material’s ambient reflection coefficient $K_a$. It is constant for each material and light combination and is calculated as follows:

$$K_a I_a$$

Each location that needs color shading will have some percentage contribution from each of these components. The color value from ambient reflection is determined by the material type of a surface and is not affected by the surface normal vector or the view direction.

### 4.3.4 Calculating Pixel Color Intensities

The Phong illumination model can be summarized with the following set of equations, componentized by color and obtained by adding up all the previously discussed contributions. The subscripts on a, s, and d (ambient, diffuse, and specular) denote a color component $r$, $g$ or $b$ (red, green, or blue) pertaining to the associated variable.

$\mathbf{LS}$ is the set of all light sources that are shining on the objects in the scene. The color values for a given pixel will likely be altered by the combined effect of all the light sources interacting with, and reflecting from, surfaces.

$I_p$ represents the shade value of the red component of the pixel color in RGB format.
$I_{pg}$ represents the shade value of the green component of the pixel color in RGB format.

$I_{pb}$ represents the shade value of the blue component of the pixel color in RGB format.

\[
I_{pr} = K_{ar} I_{ar} + \sum_{ls} L_{ls} (K_{ds_r} (I_{ls} \cdot N) I_{ls,d_r} + K_{sr} (R_{ls} \cdot V))^\alpha I_{ls,s_r})
\]

Clamp $I_{pr}$ to the range $[0, 1]$.

\[
I_{pg} = K_{ag} I_{ag} + \sum_{ls} L_{ls} (K_{dg} (I_{ls} \cdot N) I_{ls,d_g} + K_{sg} (R_{ls} \cdot V))^\alpha I_{ls,s_g})
\]

Clamp $I_{pg}$ to the range $[0, 1]$.

\[
I_{pb} = K_{ab} I_{ab} + \sum_{ls} L_{ls} (K_{db} (I_{ls} \cdot N) I_{ls,d_b} + K_{sb} (R_{ls} \cdot V))^\alpha I_{ls,s_b})
\]

Clamp $I_{pb}$ to the range $[0, 1]$.

Finally, the pixel color is obtained by converting the above values into values compatible with a 24-bit RGB format. How this process is done depends on the drawing API being used.

### 4.4 Reflection Calculation

The description of ray reflection can be expressed using the following terms:

- **N** - The normalized surface normal vector.
- **I** - The normalized incident light vector.
- **R** - The normalized reflected light vector.
- **R_{\perp}** - The component of **R** perpendicular to the intersected surface.
- **R_{\parallel}** - The component of **R** parallel to the intersected surface.
- **I_{\perp}** - The component of **I** perpendicular to the intersected surface.
- **I_{\parallel}** - The component of **I** parallel to the intersected surface.
- **\theta_{i}** - The angle that the incident light ray strikes the surface.
- **\theta_{r}** - The angle that the incident light ray reflects from the surface.
With these values, we can calculate the reflected ray $R$ as follows:

First we note that

$$\theta_i = \theta_r.$$  

It follows from this that:

$$\cos \theta_i = I_i = \cos \theta_r = R_i \tag{0}$$

$$\sin \theta_i = I_\perp = \sin \theta_r \tag{1}$$

$$R_\perp = -I_\perp \tag{2}$$

$I_\perp$ is obtained by projecting $I$ onto $N$ (see Figure 7).

The formula to project $I$ onto a normal $N$ is given by:

$$I_\perp = \frac{\mathbf{N} \cdot \mathbf{I}}{||\mathbf{N}||^2} \mathbf{N} \tag{3}$$

Since $N$ is normalized (in other words, it has a length of 1) this equation simply becomes (4):

$$I_\perp = (\mathbf{I} \cdot \mathbf{N})(\mathbf{N}) \tag{4}$$

$$R = R_i + (R_\perp) \tag{5}$$

Using equations (0), (1) and (2) we can derive (6) from (5).

$$R = I_i + (-I_\perp) \tag{6}$$

$$R = (1 - I_\perp) + (-I_\perp) \tag{7}$$

$$R = I - 2I_\perp \tag{8}$$

Using equation (4), we can rewrite (8) as

$$R = I - 2((\mathbf{I} \cdot \mathbf{N})(\mathbf{N})) \tag{9}$$

The appeal of the equation as it exists in form (9) is that it can be used with the vectors that we have already computed at the reflection stage of the ray trace algorithm.
Parallelizing a sequential algorithm involves analyzing the algorithm for code locations that can be processed in parallel. Many algorithms have more than one location that can be parallelized. In the case of the ray tracing algorithm, there are two locations within the algorithm that can be parallelized [18]. The first parallelization strategy, called PS-Ray, involves assigning a thread to the processing of each ray. PS-Ray includes all sphere and triangle intersections, as well as shading. The second, called PS-Triangle, involves parallelizing the triangle intersection segment of each ray’s trace. Parallelizing the algorithm using PS-Ray is difficult to do because the current GPU technology does not support recursion [21]. As a consequence, the initial attempt to parallelize the algorithm involved using PS-Triangle. PS-Ray was eventually accomplished by limiting the ray tracing depth so as to not need a recursive call. As a result, one ray bounce (i.e., reflection) is achieved.
5.1 STREAM PROCESSING

Stream Processing is a computational technique in which a thread-partitioned input data set is mapped to a thread-partitioned output data set. This may sound very similar to other types of multi-threaded computation. The difference lies in the restrictions placed on the computation [27]. Each partition of the input data set is processed by a single hardware thread, known as a work item in OpenCL, and mapped to its associated partition in the output data set. Each hardware thread is executing a sequence of code known as a kernel instance. A kernel is essentially a function that can have arguments passed to it. Each input/output data partition pair is completely independent from any other partition pair. This lends itself to very scalable computations because high degrees of parallelism rely on minimizing data dependencies between different threads [13]. This has the effect of freeing all threads from having to wait on any other thread’s result data, thus speeding concurrent execution. This technique is known as stream processing since the input and output data sets are referred to as streams. For GPUs, there exist two major types of data parallelism that can implement stream processing: SPMD and SIMD.

5.1.1 SPMD AND SIMD DATA PARALLELISM

SPMD and SIMD are closely related terms within the context of OpenCL programming. SPMD stands for Single Program Multiple Data. OpenCL kernels are running in “Single Program Multiple Data” mode when each thread, or processing element, operates on its own set of data and also has its own instruction pointer. SIMD stands for “Single Instruction Multiple Data”. This occurs when multiple processing elements execute the same instruction at once and share an instruction pointer [30]. The amount of instruction level parallelism possible is determined by the capabilities of the compiler as well as manual optimization by the programmer. The compiler can only generate code that contains higher levels of hardware parallelism if it can algorithmically detect the optimization opportunities. As OpenCL compilers mature, this capability will likely improve.

5.1.2 PARALLELISM IN THE RAY TRACER

In order for current GPU hardware to be most efficiently utilized, all processing elements need to execute the same instructions in lock step. If all threads, or processing elements, do not execute the same instructions, the SIMD processing becomes very inefficient. Since the code within both kernels of this project have many divergent code paths (conditional branches), each processing element will potentially need to execute instructions unique to its associated thread. In light of this fact, the parallelism model closely follows the SPMD paradigm but the GPU hardware accomplishes this feat while still using SIMD hardware. In terms of low-level hardware implementation, the graphics hardware is running multiple threads in a SIMD lock-step fashion and uses thread masking when branches occur. Thread masking can be thought of as the way a particular thread ignores (e.g., NOPs) an instruction.
When a branch is encountered, the threads that do not take the branch do not accumulate the effects of the branches’ instructions (i.e., the instructions are masked) and the threads that do take the branch are affected by the instructions in the branch.

5.2 **Overview of OpenCL**

OpenCL’s programming API was used to parallelize the ray tracing algorithm. It stands for Open Computing Language and is described by the Khronos Group as a programming framework for heterogeneous compute resources. This implies that one can write an OpenCL program and can compile and run it against a GPU or a CPU of any supported type with no necessary code changes. The framework provides a way for a programmer to access all the compute resources in a system instead of letting some kinds of processors sit relatively idle. Even today, idleness is typical of GPUs when a game or other graphically intense application is not running on a computer system. Each processor vendor is responsible for providing its implementation of OpenCL.

There are two areas of OpenCL relevant to this project, its Memory and Execution Model. We will now cover both.

5.2.1 **OpenCL Memory Model**

![OpenCL Memory Model](image)

**FIGURE 8 - OPENCL MEMORY MODEL**

The different types of memory in the OpenCL Memory Model are depicted in Figure 8 and may be described as follows:
Global Memory – A type of memory visible to all work items [2], [4], [5]. A work item can read and write to this memory region. This region is where all the parameters in this project are initially written. This is the slowest type of memory.

Local Memory – A memory region that is only visible to the work items in a work group [2], [4], [5]. This can be thought of as a programmer-controlled cache that is usually less wasteful than a hardware-controlled cache. This type of memory is faster than global memory but not as fast as registers.

Private Memory – A type of memory only visible to an individual work item [2], [4], [5]. Registers are primarily used for this type of memory. Registers are the fastest type of storage.

Most of the kernel parameters in this project are initially placed in Global Memory and are moved to Private Memory when certain global array values get assigned to local variables. This is done to increase the utilization of registers and hence the speed of computation.

5.2.2 OpenCL Execution Model

The topic of OpenCL's execution model is large, and much of the subject matter is beyond the scope of this thesis. The following subsections provide a brief explanation of the parts of the OpenCL Execution Model that are necessary to understand this project. Some relevant terms are defined below [4]:

Host: The host program is the client code that interacts with objects defined by OpenCL to accomplish some computational task [4]. The host compiles and orchestrates the execution of kernels.

Device: The OpenCL device, or compute device, is where functions (kernels) execute. This device is a GPU graphics card in this project, but it can be any type of processor as long as OpenCL is implemented by the processor vendor [4].

Kernel: A kernel is a function written in the OpenCL ISO 99-based C Language and compiled with the OpenCL compiler [4]. For each kernel executed, multiple kernel instances run in parallel on a device. There is one kernel instance associated with each thread.

Memory Object: A memory buffer visible to OpenCL devices [4]. This term “object” should not be confused with the concept of an object in the object-oriented programming paradigm.

Command Queue: All interaction between the host and the OpenCL devices occurs through commands. The three types of commands are kernel execution, memory read/write, and kernel synchronization commands [4].
**Context:** A context defines a specific combination of devices, kernels, memory objects, and program objects. It can be thought of as the environment in which the kernels execute [4].

In the following sections, we’ll cover some of these concepts in more detail. We will do so within the context of three ideas that all programmers are familiar with:

1) Compiling the kernel  
2) Allocating memory for kernel arguments  
3) Executing the kernel

These 3 steps will now be described in OpenCL terminology.

### 5.2.2.1 Compiling the Kernel

*Program objects* are the objects that provide access to the OpenCL compiler to compile C-like code. When the compile function is invoked on the program object, the kernel (function) code is compiled for every device grouped with the same context that the program object is grouped with [4]. From the program object a kernel object can be obtained. The kernel object encapsulates the compiled kernel function declared in your program and the arguments that will be used in the kernel. The arguments will be associated with the kernel after they have been created.

### 5.2.2.2 Allocating Memory for Kernel Arguments

OpenCL memory objects are allocated through functions on a context object, and all devices associated with that context object can read and write to the memory referenced by the memory objects. The type of OpenCL memory objects used in this project are *buffer objects*. These buffer objects are one-dimensional arrays of a particular data type. The data type can be any scalar data type, a user-defined structure, or a vector data type. The data type used in this project’s code is the `float` type. The buffer objects can reside either in the host memory or the device memory and are used to store the data that is transferred between them [4]. The allocated memory object(s) are used as kernel arguments when the kernel is executed. They are associated with the kernel object by API calls that tie the arguments to the kernel.

### 5.2.2.3 Executing the Function

Having carried out the prior steps, the programmer is ready to execute the kernel. Each device in a system that is targeted for execution of a kernel will have to have a command queue created for it [4]. In this project, a command queue is created for the GPU only. This command queue is the place where we issue the following commands:
• **Parameter-write memory commands** - Each one of these memory commands essentially writes the kernel arguments to the device in preparation for kernel execution. These memory write calls are made asynchronously.

• **Kernel invocation command** - This asynchronous command executes the kernel on the computation device.

• **Result-read memory command** - This command is for retrieving the data from the GPU device.

• **Synchronization command** - This call blocks (i.e., does not complete) until all previous asynchronous commands have finished. Its purpose is simply to make sure all work has completed before the host attempts to read the result data. Basically, this is accomplished by waiting on event objects that were passed along with each of the previous commands. A detailed discussion of event objects is beyond the scope of this thesis.

Having covered the conceptual aspects of executing a kernel function on a device using OpenCL, we now examine some sample code written in JOCL, a Java interface to OpenCL.

### 5.2.3 Executing a Kernel In JOCL

The complete set of steps required to execute a kernel are as follows:

1. Create a context.

   ```java
m_clContext = CLContext.create();
```

2. From the context object, retrieve the GPU device with the highest FLOPS (floating point operations per second). In the code below, notice that if the system doesn’t happen to have a GPU, the fastest CPU in the system will be retrieved.

   ```java
   m_clDevice = m_clContext.getMaxFlopsDevice(CLDevice.Type.GPU);
   if(m_clDevice == null)
   {
       m_clDevice = m_clContext.getMaxFlopsDevice(CLDevice.Type.CPU);
   }
   ```

3. From the device object, create a command queue for the device. Profiling enables timing of specific queue operations like reading and writing memory objects to and from a device as well as timing of code execution. Profiling enabled the capture of the timings for this project.

   ```java
   m_clQueue =
   m_clDevice.createCommandQueue(CLCommandQueue.Mode.PROFILING_MODE);
   ```
4. Open a file stream that points to the source code for the kernel. Raytrace.cl is the name of the C source file that contains the kernel for this example.

```java
File directory = new File(".";
String path = directory.getCanonicalPath();
path = path + "/Objects/raytrace.cl";
InputStream stream = new FileInputStream(path);
```

5. Now it is necessary to compile the stream that has the ray trace code in it. From the context object, invoke createProgram, passing the code stream. This will create the program object. Notice that compilation of OpenCL code happens at runtime.

```java
m_clProgram = m_clContext.createProgram(stream).build("");
```

6. From the program object, invoke createCLKernel, passing the name of the kernel as specified in the code. This will create the kernel object. The kernel function prototype from raytrace.cl is listed below the createCLKernel call to show that the name of the kernel passed into the createCLKernel method is the same name as that of the kernel function prototype.

```java
m_clKernel = m_clProgram.createCLKernel("RayTrace");

__kernel void RayTrace(global float* rayData, int numRays, …
```

7. From the context object, create buffers for all the kernel parameters. Since all the buffers are created from the context, OpenCL and all devices associated with the context know about the OpenCL memory objects. The memory can be easily shared between devices belonging to the same context.

```java
CLBuffer<FloatBuffer> lightData =
    m_clContext.createFloatBuffer((fg.lightDataSize * fg.numLights)+1,
    CLMemory.Mem.READ_ONLY);
CLBuffer<FloatBuffer> sphereData =
    m_clContext.createFloatBuffer(fg.sphereDataSize * fg.numSpheres,
    CLMemory.Mem.READ_ONLY);
CLBuffer<FloatBuffer> triangleData =
    m_clContext.createFloatBuffer(fg.triangleDataSize * fg.numTriangles,
    CLMemory.Mem.READ_ONLY);
CLBuffer<FloatBuffer> sceneState = m_clContext.createFloatBuffer(4,
    CLMemory.Mem.READ_ONLY);
CLBuffer<FloatBuffer> viewMat = m_clContext.createFloatBuffer(16,
    CLMemory.Mem.READ_ONLY);
CLBuffer<FloatBuffer> modelMats = m_clContext.createFloatBuffer(16 *
26

fg.numSpheres, CLMemory.Mem.READ_ONLY);
CLBuffer<FloatBuffer> inverseTransposes = m_clContext.createFloatBuffer(16 *
fg.numSpheres, CLMemory.Mem.READ_ONLY);
CLBuffer<FloatBuffer> rayDataCL = m_clContext.createFloatBuffer(numRays *
6, CLMemory.Mem.READ_ONLY);
CLBuffer<FloatBuffer> colorData = m_clContext.createFloatBuffer(3 *
numRays, CLMemory.Mem.WRITE_ONLY);

8. Populate all the buffers with data. For brevity, only one buffer is populated in the code sample.
All the other buffers can be populated in a similar manner. This involves copying the view matrix
to the CLBuffer object that was allocated in the step above.

```java
int c = 0;
for (c = 0; c < 16; c++)
{
    viewMat.getBuffer().put(c, fg.viewMatf[c]);
}
```

9. From the kernel object, invoke putArg and/or putArgs, passing the buffers previously created
in step 7. This notifies OpenCL of the mapping between buffers and kernel parameters. The order
of the buffers from left to right is the same order as is present in the kernel from left to right.

```java
m_clKernel.putArg(rayDataCL).putArg(numRays).putArgs(modelMats, viewMat,...
```

10. From the queue object, invoke putWriteBuffer once for each buffer object. This queues the
buffer contents that will be sent to the device. All the putWriteBuffer calls are made
asynchronously, and all the calls are synchronized later by invoking a blocking wait on the queue
for all the writes’ associated events.

```java
m_clQueue.putWriteBuffer(rayDataCL, false, l);
m_clQueue.putWriteBuffer(modelMats, false, l);
m_clQueue.putWriteBuffer(viewMat, false, l);
m_clQueue.putWriteBuffer(inverseTransposes, false, l);
m_clQueue.putWriteBuffer(sceneState, false, l);
m_clQueue.putWriteBuffer(sphereData, false, l);
m_clQueue.putWriteBuffer(triangleData, false, l);
m_clQueue.putWriteBuffer(lightData, false, l);
```

11. Calculate the local and global work size for the kernel. In OpenCL, the global work size has to be a
multiple of the workgroup size.

```java
double localWorkSize = numRays;
localWorkSize = Math.ceil(localWorkSize);
localWorkSize = Math.min(localWorkSize, m_clDevice.getMaxWorkGroupSize());
int globalWorkSize = roundUp((int)localWorkSize, (int)numRays);
```
12. From the queue object, invoke put1DRangeKernel asynchronously, passing the local work size, the global work size, and the kernel object. This command will execute the kernel.

   m_clQueue.put1DRangeKernel(m_clKernel, 0, (int)globalWorkSize, (int)localWorkSize, l);

13. From the queue object, invoke putReadBuffer asynchronously to retrieve the color data.

   m_clQueue.putReadBuffer(colorData, false, l);

14. From the queue object, invoke putWaitForEvents to wait for all the above asynchronous work to finish. This is conceptually similar to a thread join.

   m_clQueue.putWaitForEvents(l, true);

5.2.4 OPENCL ISSUES

While the creators of OpenCL claim it has the ability to seamlessly compile and run the same code on different processor architectures, the reality is just slightly different. If a piece of software is written that is “type compatible” with all the architectures for which compilation is intended, then there may be no difficulties compiling across different processor types. However, if the code contains data types that are not supported by the particular processor for which code is to be compiled, the code will fail to compile. This scenario occurred in this project. The double type is not supported on the AMD Radeon Mobility 5870. As a consequence, all the kernels’ double types had to be changed to float types. The data buffers being sent from the host had to be changed to the float type as well. In the opinion of the author, the use of floats caused no perceptible loss in the visual quality of the images produced in this project.

5.3 IMPLEMENTING PS-TRIANGLE IN AN SPMD KERNEL

The sequential ray tracing algorithm that served as the basis for this parallelization iterates through a list of triangles one at a time in an attempt to determine whether a ray has intersected with one or more of them. The OpenCL parallelization of this portion of the algorithm essentially tests for intersections with all the triangles in a given object using the GPU’s hardware parallelism. The algorithm determines whether a ray pierces an object’s bounding sphere and then passes all the triangle and ray information to the triangle intersection kernel if the bounding sphere was intersected by the ray. The results obtained from the triangle intersection kernel are a reduction of the input stream of triangles into a \( (t, u, v) \) parameter set for each triangle. Recall from the ray definition that \( t \) is the parameter value used by the parametric ray equation to determine a point (in this case, the intersection point) on a ray. \( u \) and \( v \) are the
parameters that were derived in the discussion of triangle intersection. Only triangles with intersections will have positive t values. The other triangles will be given values of 0 for t.

5.3.1 Algorithm Design

The design of the triangle intersection kernel involved moving only the triangle intersection segment of the ray tracing algorithm to the kernel. The flowchart of the design can be seen in Figure 9.
Recall that in order to perform the triangle intersection parallelization, it is necessary to first check whether the ray pierces the object’s bounding sphere. If the ray has pierced the object’s bounding sphere,
we send all the data that is necessary to execute the triangle intersection code. The data format is detailed below.

5.3.2.1 Ray Data Format

The ray data is arranged in its buffer as illustrated in Figure 10. The ray direction vector is normalized. This data is passed into the kernel as an argument residing in global memory but gets copied into private memory near the beginning of the kernel code.

5.3.2.2 Triangle Data Format

In addition to the ray, we need to pass the triangle data to the triangle intersection kernel. Figure 11 shows the layout of this data.

5.3.2.3 Output Stream Format

Once the input streams have been passed to the triangle intersection kernel, each hardware thread attempts to intersect the ray with each triangle in parallel. An output stream is generated comprised of the values \( t, u, \) and \( v \). Figure 12 shows the structure of the output stream.

The triangle intersection output stream is transferred back to the host device where the \( t, u, \) and \( v \) values for each triangle are evaluated. There may be multiple triangles that were intersected, and we only want the closest one. The algorithm incurs a cost here because the \( t, u, \) and \( v \) values have to be searched until
the \((t, u, v)\) set with the smallest positive \(t\) value is found. When the closest \(t\) value is found, it is used to calculate the intersection point with the triangle using the ray equation. Triangles that the ray did not intersect will be assigned 0 for their \(t\) values.

5.3.3 **CACHING TRIANGLE DATA STRUCTURES**

The triangle data structures do not change at all during the entire ray trace algorithm. This allows one to make the copy of data across the PCI Express bus more efficient. When attempting to write an unchanged data buffer to a device, the data is not copied on the second and subsequent write operations. This effectively means that the triangle data may be cached on the GPU device after it is first transferred. The speed of the parallelization of the triangle intersection segment of the algorithm is greatly increased due to this fact. This triangle caching phenomenon can be seen in the graph of Figure 22.

5.4 **IMPLEMENTING PS-RAY IN AN SPMD KERNEL**

The process of implementing the entire ray tracer in the kernel requires that the host application restructure all the necessary data so that it can be passed in kernel parameters. The output from the kernel is the set of 24-bit RGB values whose corresponding pixel colors must be displayed on the screen.

5.4.1 **ALGORITHM DESIGN**

The design of the PS-Ray kernel involved placing most of the ray trace code into a kernel and limiting the ray tracing algorithm to a single reflection. The general overview of the algorithm can be seen in Figure 13.
Figure 13 - Ray Trace Parallelization

1. Calculate rays for the entire scene and put them in an OpenCL buffer. Put all geometry and material in an OpenCL buffer. Send data to the device and execute the kernel.

2. For each ray in parallel:
   - Attempt to intersect ray with the next bounding sphere in a loop.
   - Check for intersections against all triangles inside the bounding sphere.
   - Did the ray intersect a triangle?
     - Yes: If this triangle intersection is the closest to the viewer so far, keep track of it as the closest intersection.
     - No: If not shadowed, shade the intersection point based on local specular, diffuse, and ambient contribution. Add reflection contribution.

3. When done looping through spheres:
   - Found a closest intersection point?
     - Yes: Shade the point with the background color. The ray missed all geometry.
     - No: If done, return to step 1.

4. Write the pixel value to this work item's output buffer.

5. Host reads the pixel buffer and writes data to the screen.
5.4.1.1 Ray Data Layout

In the PS-Ray kernel, all the rays for the entire screen are sent to the kernel. Once an instance of kernel execution has begun, each thread makes a function call to obtain its thread ID. The thread ID is used to calculate an offset into the ray data structure to retrieve the appropriate ray data for the thread. In this way, each hardware thread processes one ray and produces a pixel color as output. Figure 14 illustrates the ray data layout in the ray buffer. This data begins in global memory and is transferred into private memory near the beginning of the kernel code.

![Ray Data Layout](image)

**Figure 14 - Ray Data Layout for Ray Trace Kernel**

5.4.1.2 Sphere and Triangle Data Layout

The next data structure of importance contains the bounding sphere data. This data structure contains all the necessary information to do a sphere-intersection calculation. In addition, it contains two offset values. The first offset value is the starting location of the embedded polygonal mesh’s triangles which reside in the triangle buffer that is discussed below. The second value is the ending offset of the same set of triangles. This enables the program to rapidly look up the appropriate set of triangles when an intersection with a bounding sphere has occurred. Figure 15 details the sphere data structure layout. It is a large contiguous float array.
The layout of the triangle data is shown in Figure 16. Notice that the vertex normal vectors are provided along with the vertices. These are the same vertex normal vectors that were used earlier in the discussion of Phong shading.

The above data structures comprise the input data stream. In the PS-Ray kernel, this input data stream is processed using the modified version of the ray tracing algorithm. After this processing is finished, the pixel data for the screen will have been written into the output stream. The output stream is an array of pixel colors. The format of these pixels is shown in Figure 17.
This pixel output stream is transferred back to the host process and drawn to the screen using OpenGL’s 2-D drawing capabilities.

6  AMD RADEON MOBILITY 5870 GPU

The hardware specifications of the graphics card can dramatically affect the resulting timings. The description of the hardware responsible for performing the calculations is provided below. The particular GPU hardware used is the AMD Radeon Mobility 5870 [3]:

6.1  HARDWARE SPECIFICATIONS

- 1.04 billion 40nm transistors
- 800 Stream Processing Units
- GDDR5 memory interface
- PCI Express 2.1 x16 bus interface
- Engine clock speed: 700 MHz
- Processing power (single precision): 1.12 TeraFLOPS
- Data fetch rate (32-bit): 112 billion fetches/sec
- Memory clock speed: 1.0 GHz
- Memory data rate: 4.0 Gbps
- Memory bandwidth: 64 GB/sec
- Memory size: 1024 MB
- Thermal Design Power: 50 Watts

6.2  MEMORY CONSIDERATIONS

There are two aspects of the Radeon Mobility 5870’s memory architecture which limit the number of threads that can be executing at a given moment. One is the number of registers in use. The other is the amount of local data share per compute unit. On the Radeon Mobility 5870, here are the available quantities of each:

- 256KB of registers per compute unit.
- 32KB of local data share per compute unit.

6.3  MAPPING THE RADEON MOBILITY 5870 TO THE OPENCL MEMORY MODEL

The implementation of the OpenCL Memory Model is dependent on the particular device on which the OpenCL code will be executed. Figure 18 shows an approximate mapping of the Radeon Mobility 5870 hardware to the OpenCL memory model [29].
Results for this project were gathered for PS-Ray, PS-Triangle, and the single-threaded approach. In one graph, a comparison is drawn across the timings of PS-Triangle, the single-threaded triangle intersection code, and PS-Ray. The intent of this graph is to show the degree of speed-up achieved for the two different parallelization attempts. The graph is shown in Figure 20. Notice that the PS-Ray kernel achieved such an improvement that the chart x-axis had to be displayed using a logarithmic scale in order for the PS-Ray kernel timings to be visible. The two other graphs of interest are the charts that detail the kernel memory transfer times for both PS-Ray and PS-Triangle. We can see that the memory transfer times of PS-Triangle are orders of magnitude larger than the memory transfer times for PS-Ray. These timings are shown in Figure 21 and Figure 22.
FIGURE 19 - REFLECTIONS ON THE TEAPOT FOR BOTH HANDLES AND THE SPOUT
FIGURE 20 - COMPARING TIMINGS OF PS-RAY AND PS-TRIANGLE TO SINGLE-THREADED TRIANGLE INTERSECTION
7.1 Single-threaded Triangle Intersection

The single-threaded triangle intersection timings were obtained as a baseline comparison against both the PS-Triangle kernel and the PS-Ray kernel.
7.2 Parallel Strategies versus Single-threaded Triangle Intersection

The PS-Triangle kernel was able to decrease the time to intersect objects substantially. At the high end of the polygon count, overall improvements in speed went from 1,774,450 milliseconds to 792,082 milliseconds, a speed-up of 224% for the crocodile when comparing the single-threaded triangle intersection routine to PS-Triangle. However, the crocodile intersection code embedded in the PS-Ray kernel took at most 12,628 milliseconds. This means that the speed-up for the intersection code embedded in the PS-Ray kernel was at least 14051% faster than the single-threaded intersection code. This clearly demonstrates the enormous processing throughput of GPUs. Note in Figure 20 that at the low end of the polygon count, the setup and memory transfer overhead of PS-Triangle resulted in a situation where the single-threaded intersection was actually faster than PS-Triangle.

8 Future Work

There are a number of ways in which the kernel execution speeds in this project may be optimized. These include:

- Implementing more advanced data structures to optimize triangle intersection.
- Implementing the ray trace kernel iteratively to allow more ray reflections.
- Optimizing the kernels to use specialized functions and data types within the OpenCL language to attempt to utilize more SIMD hardware – in other words, performing fine-grained kernel optimization.
- Attempting to access the frame buffer within the OpenCL kernel so that the pixel data does not have to be transferred back to the host for drawing.
- Storing all scene data in a texture to take advantage of caching. Reads from global memory are minimally cached on the Radeon Mobility 5870.

9 Conclusions

It is very clear that parallelizing the ray tracing algorithm on GPU hardware leads to large speed-ups. There are speed-ups for both PS-Triangle and PS-Ray. Unfortunately, even though speed-ups are possible in both scenarios, the programmer is forced to choose one parallelization strategy or the other because to the best of the author’s knowledge, nested kernel calls are not possible. An ideal solution would be to parallelize using one thread per ray and then launch another kernel to handle the triangle intersection segment of the ray thread [24]. The ability to invoke a stream-processing kernel from within another stream-processing kernel may not be possible but it would address the issue of having to give up some degree of parallelism to get more elsewhere. In other words, it is clear that although PS-Ray is much
faster, further speed-ups gained by PS-Triangle are not realized because one cannot execute a kernel within a kernel, or nested kernel execution, using OpenCL [24].

There are, however, indications that OpenCL technology may be able accomplish nested kernel execution soon. One of these indications is the fact that technologies like OpenMP and NVidia’s Kepler already support launching threads within threads and kernels within kernels, respectively. It does not seem like a large conceptual or technical leap to extend this idea to OpenCL kernels. The difficulty would appear to lie in making this process seamless and cross-platform to the developer, given the current hardware separation between CPUs and GPUs. That being said, it does appear that the underlying processor technology is moving in a direction that may make this possibility a reality. This includes current attempts by AMD to fuse the GPU and CPU cores on a single processor die as well as to unify the memory space accessed by these two processor types [11]. Intel has also stated that it plans on adding more graphics capability to its processor dies as well. With this tighter integration of memory and processor hardware, making the distinction between launching threads within a thread and launching a kernel within a thread may become unnecessary.

References


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